

$$25) \frac{\tan \theta}{\tan \theta} + \frac{\tan \theta}{1 - \sec \theta} = \frac{\tan \theta(1 - \sec \theta)}{\tan \theta(1 - \sec \theta)} = \frac{\tan \theta(1 - \sec \theta)}{\tan \theta(1 - \sec \theta)} = \frac{\tan \theta(1 - \sec \theta)}{\tan \theta(1 - \sec \theta)}$$

$$= -\frac{2 \sec \theta}{\tan \theta} = -\frac{2}{\cos \theta} \cdot \frac{\cos \theta}{\sin \theta} = -\frac{2}{\sin \theta} = -2 \csc \theta$$

$$26) \frac{\cos u}{\cos u - \sin u} = \frac{\cos u}{\cos u - \sin u} \cdot \frac{\frac{1}{\cos u}}{\frac{1}{\cos u}} = \frac{1}{1 - \frac{\sin u}{\cos u}} = \frac{1}{1 - \tan u}$$

$$27) (\sec v + \tan v)^2 = \sec^2 v + 2 \sec v \tan v + \tan^2 v = \frac{1}{\cos^2 v} + \frac{2 \sin v}{\cos^2 v} + \frac{\sin^2 v}{\cos^2 v} = \frac{1 + 2 \sin v + \sin^2 v}{\cos^2 v} = \frac{(1 + \sin v)^2}{1 - \sin^2 v} =$$

$$\frac{(1 + \sin v)^2}{(1 - \sin v)(1 + \sin v)} = \frac{1 + \sin v}{1 - \sin v}$$

$$28) \frac{\cos u}{1 + \tan u} - \frac{\sin u}{1 + \cot u} = \frac{\cos u}{1 + \frac{\sin u}{\cos u}} - \frac{\sin u}{1 + \frac{\cos u}{\sin u}} = \frac{\cos^2 u}{\cos u + \sin u} - \frac{\sin^2 u}{\sin u + \cos u} = \frac{\cos^2 u - \sin^2 u}{\cos u + \sin u} =$$

$$\frac{(\cos u - \sin u)(\cos u + \sin u)}{\cos u + \sin u} = \cos u - \sin u$$

$$29) \frac{\cot u + \csc u - 1}{\cot u - \csc u + 1} = \frac{\cot u + (\csc u - 1)}{\cot u - (\csc u - 1)} = \frac{\cot u + (\csc u - 1)}{\cot u - (\csc u - 1)} \cdot \frac{\cot u + (\csc u - 1)}{\cot u + (\csc u - 1)} =$$

$$\frac{\cot^2 u + 2 \cot u(\csc u - 1) + (\csc^2 u - 2 \csc u + 1)}{\cot^2 u - (\csc^2 u - 2 \csc u + 1)} = \frac{\csc^2 u - 1 + 2 \cot u(\csc u - 1) + (\csc^2 u - 2 \csc u + 1)}{\csc^2 u - 1 - (\csc^2 u - 2 \csc u + 1)} =$$

$$\frac{2 \csc^2 u - 2 \csc u + 2 \cot u(\csc u - 1)}{-2 + 2 \csc u} = \frac{2 \csc u(\csc u - 1) + 2 \cot u(\csc u - 1)}{2(\csc u - 1)} = \frac{2(\csc u + \cot u)(\csc u - 1)}{2(\csc u - 1)} = \csc u +$$

$\cot u$

$$30) \frac{\tan u + \cot u}{\tan u - \cot u} = \frac{\frac{\sin u}{\cos u} + \frac{\cos u}{\sin u}}{\frac{\sin u}{\cos u} - \frac{\cos u}{\sin u}} = \frac{\frac{\sin^2 u + \cos^2 u}{\cos u \sin u}}{\frac{\sin^2 u - \cos^2 u}{\cos u \sin u}} = \frac{\sin^2 u + \cos^2 u}{\sin^2 u - \cos^2 u} = \frac{1}{\sin^2 u - \cos^2 u}$$